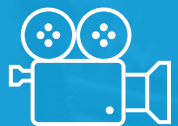


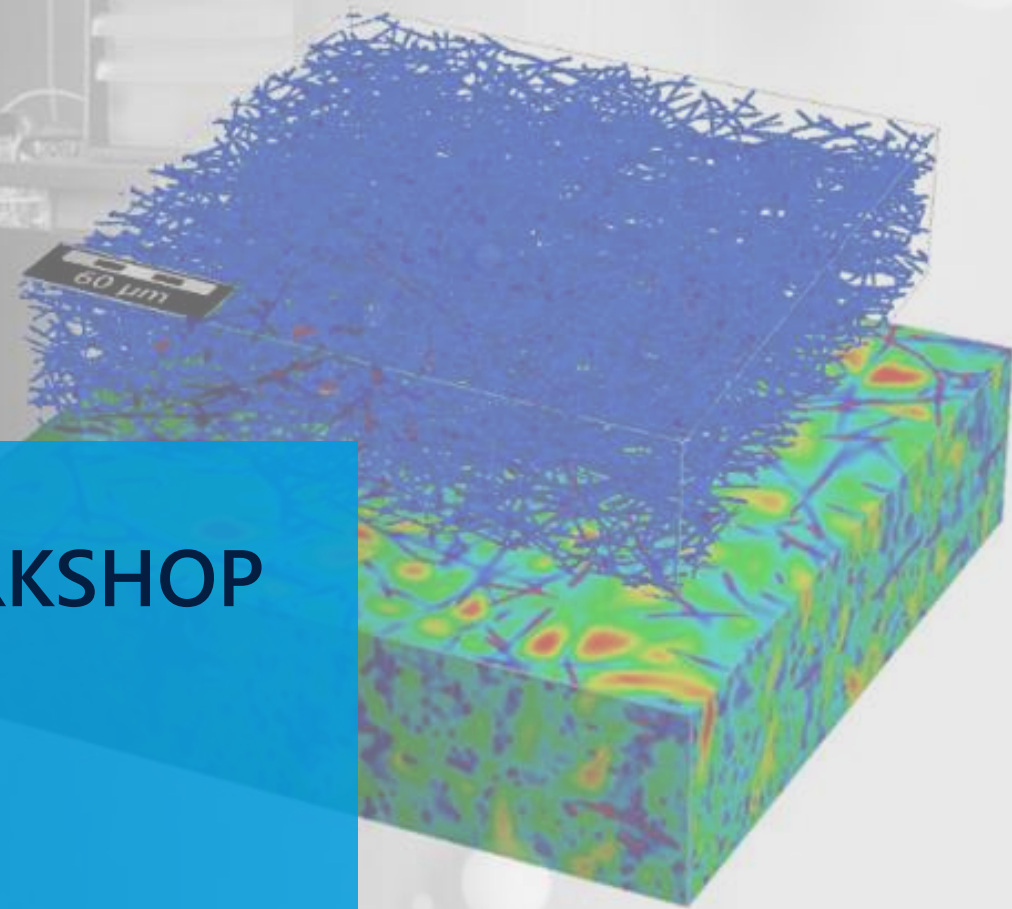
# WELCOME TO RIGAKU VIRTUAL WORKSHOP

## DEEP DIVE: FILTRATION ANALYSIS

### 3. Filtration Simulations



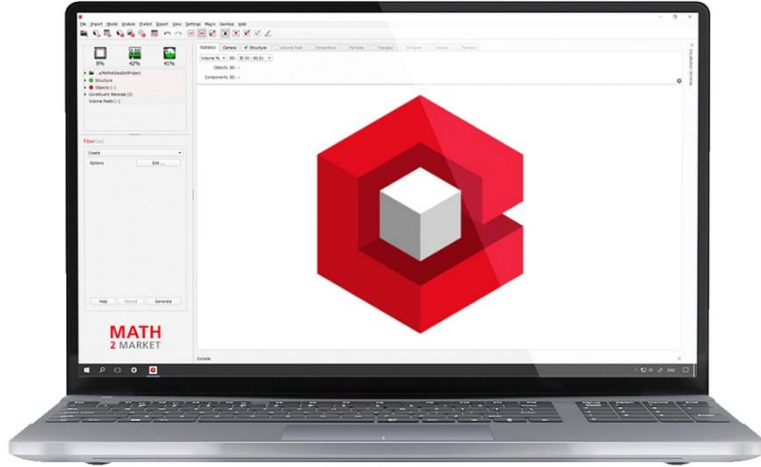
*Watch the recording*



Presenter: **Angela Criswell** | Senior Scientist

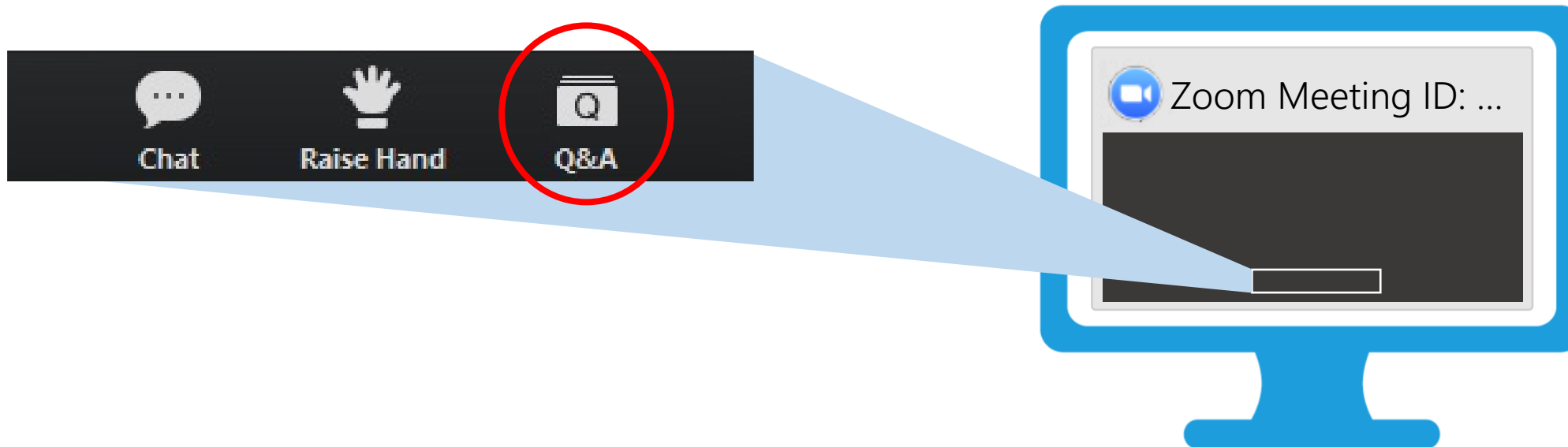
Co-presenter: **Aya Takase** | Director of X-ray Imaging

Host: **Tom Concolino** | Analytical X-Ray Consultant



**GEO DICT**  
The Digital Material Laboratory

**Philipp Eichheimer, Ph.D.** | Math2Market  
Application Engineer



You can ask questions during the presentation.  
We might turn on your microphone for further discussions.



Recording will be available tomorrow.

# *Filtration Analysis – 3. Filtration simulations*

Virtual Workshop presented by Angela Criswell

# FILTRATION ANALYSIS SERIES

1. Data collection
2. Segmentation and property analyses
3. Filtration simulations

# THINGS WE'LL COVER

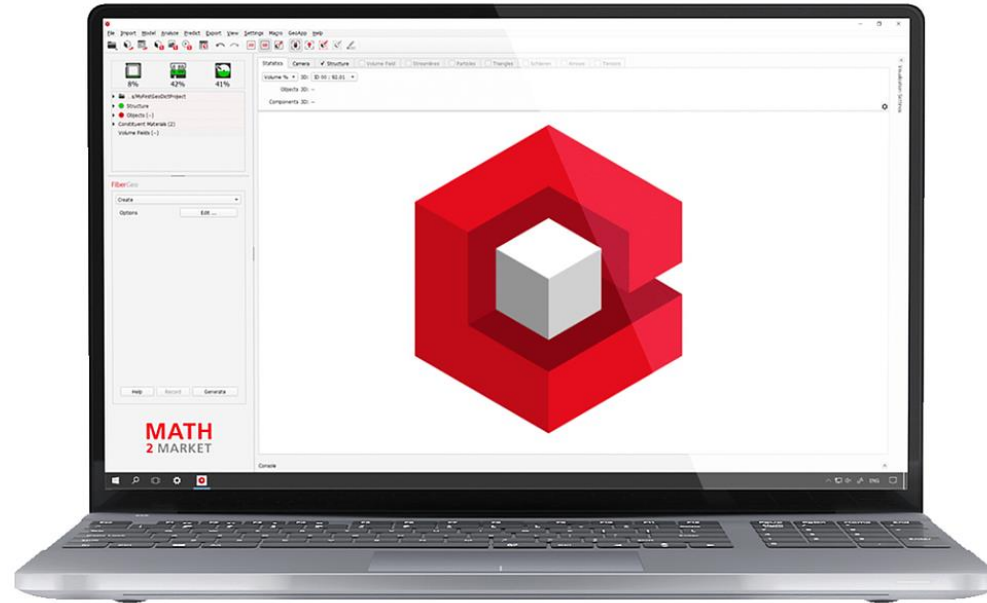
- How to simulate the filtration process for filter media
- How to track particles during filtration simulations
- How to examine filter efficiency and filter life time





## **nano3DX by Rigaku**

High resolution and high contrast for soft materials

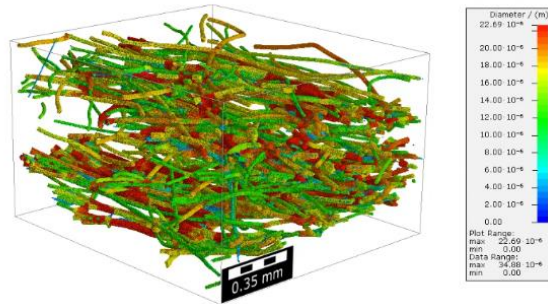


# GeoDict by Math2Market

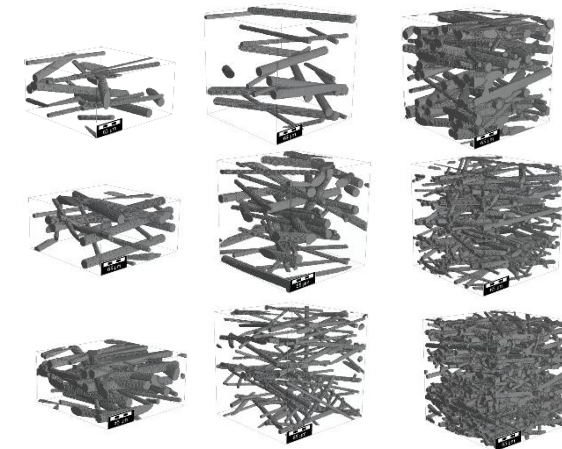
## The Digital Material Laboratory



CT data



Filter media analysis



Filter media modeling

# Filter optimization



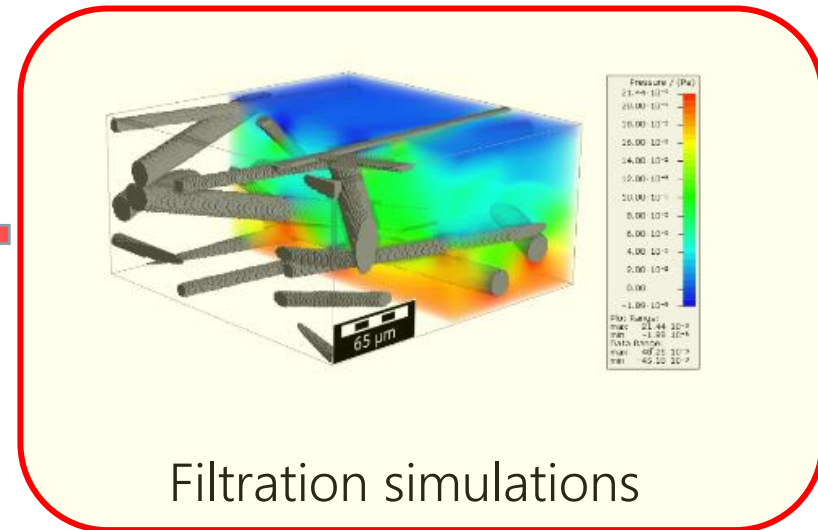
Testing

<http://www.tsi.com>



Manufacturing

<http://www.airfilterusa.com> , <http://www.zoro.com>

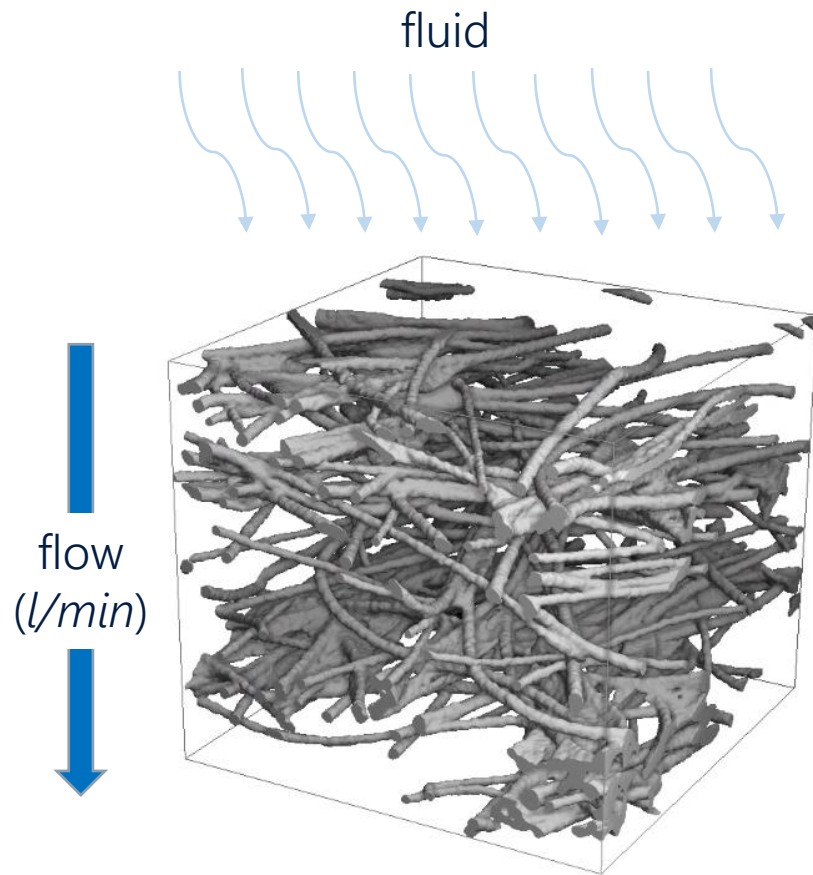


Filtration simulations



# HOW DO WE SIMULATE FILTRATION?

# FILTRATION SIMULATION

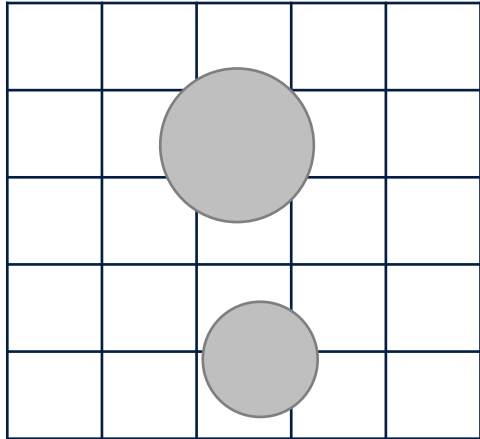


- Fluid flow
- Particle tracking
- Clogging and resistivity models

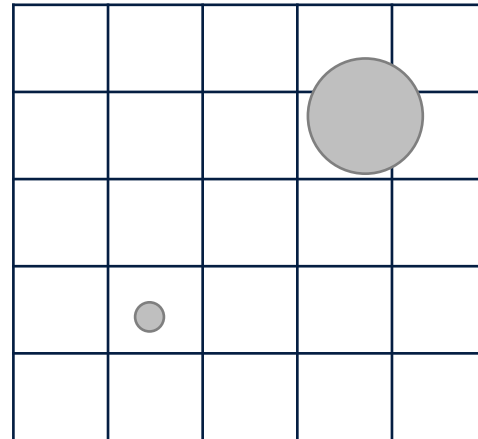
# FLUID FLOW

- Navier-Stokes
  - Pores are resolved
- Navier-Stokes-Brinkman
  - Pores are not resolved

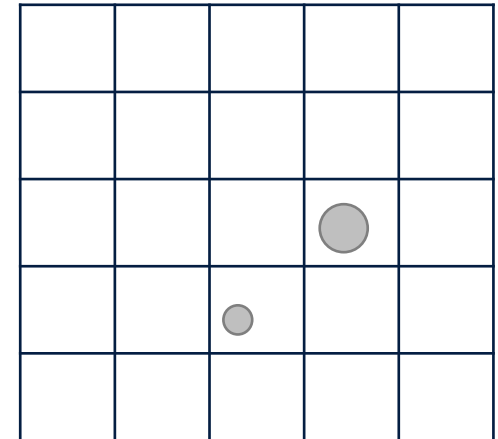
# RESOLVED VERSUS UNRESOLVED



Resolved particles



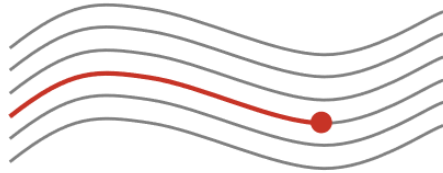
Partially resolved particles



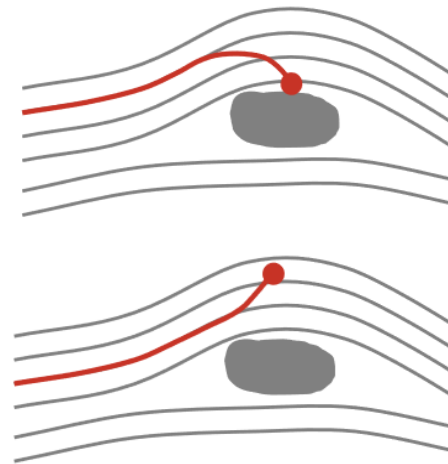
Unresolved particles

# PARTICLE TRACKING

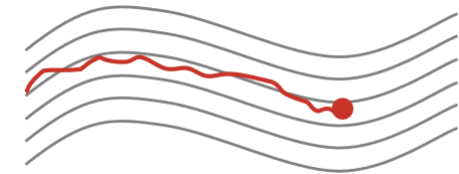
Drag flow



Electrostatic effects

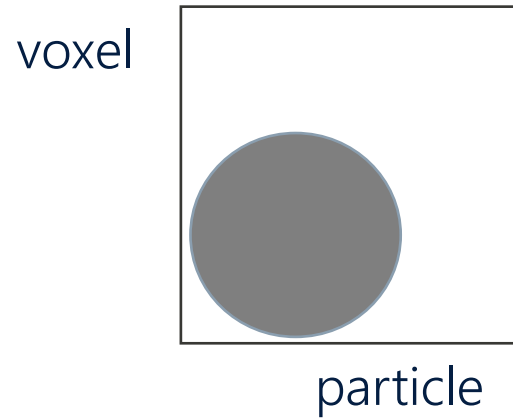


Diffusive (or Brownian) motion



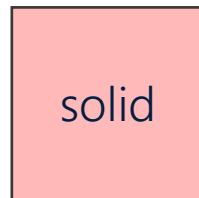


# CLOGGING AND RESISTIVITY MODEL



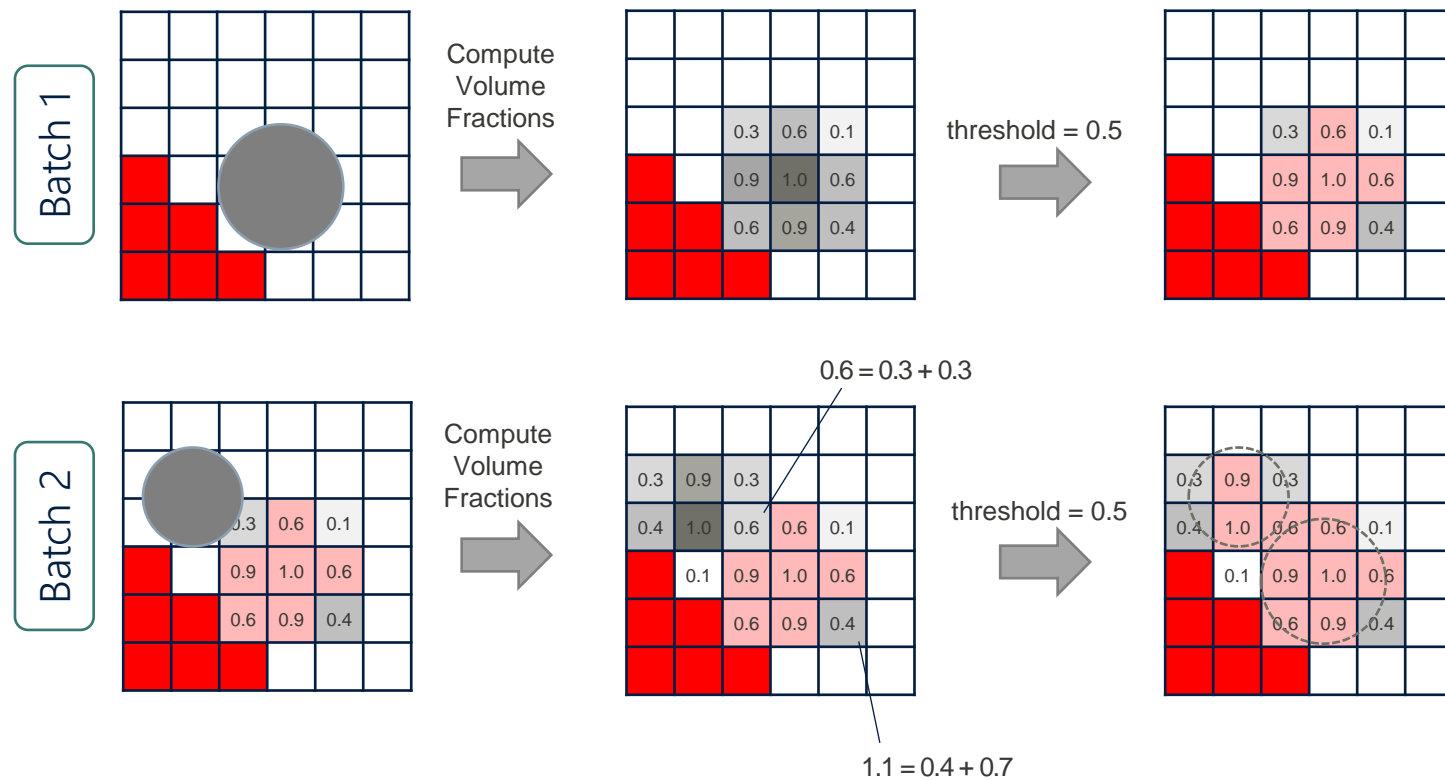
$$fill = \frac{v_{particle}}{v_{voxel}}$$

$$threshold < fill < threshold$$



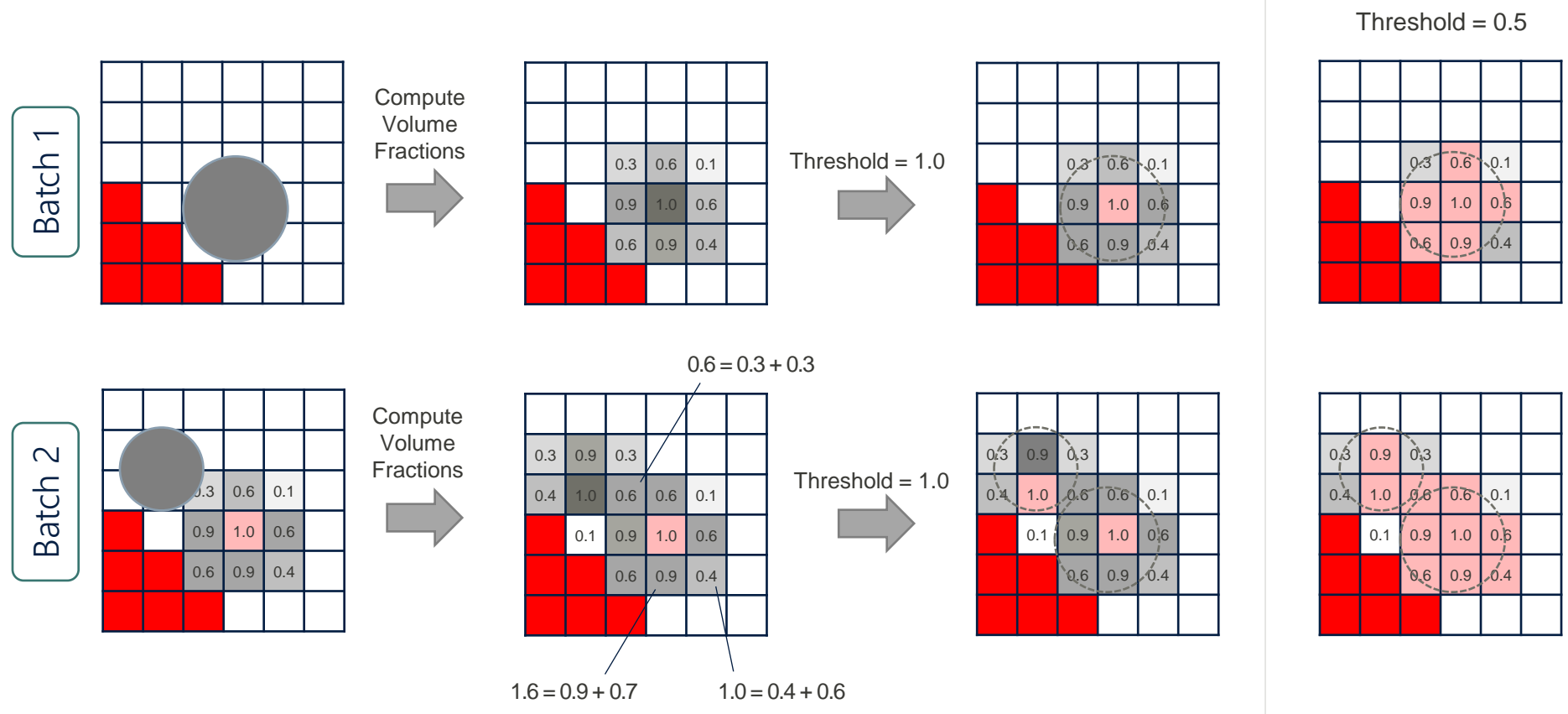
# CLOGGING AND RESISTIVITY MODEL

- Resolved (threshold = 0.5)



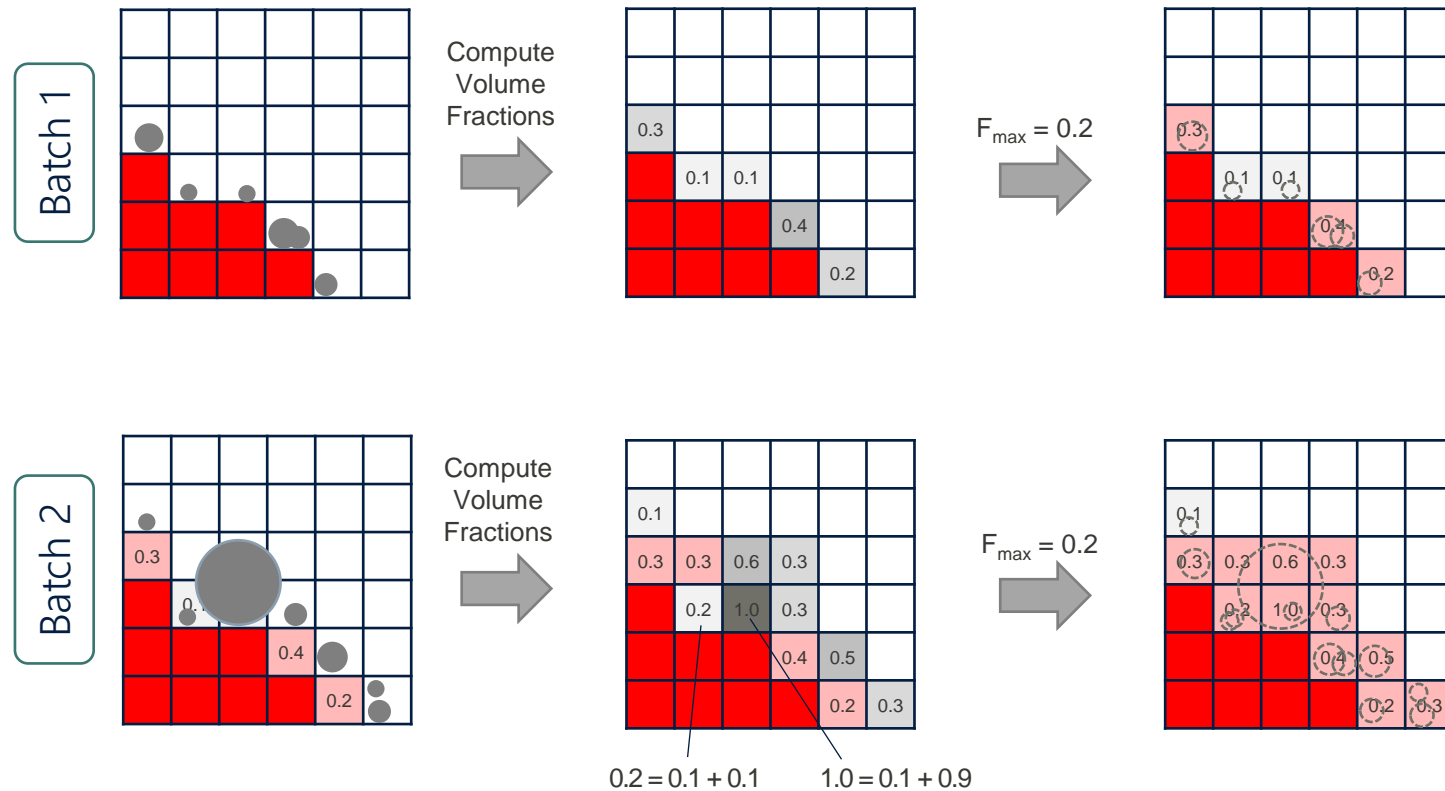
# CLOGGING AND RESISTIVITY MODEL

- Resolved (threshold = 1.0)



# CLOGGING AND RESISTIVITY MODEL

- Unresolved ( $F_{\max}$ )



# COLLISION MODELS

- Caught on first touch
- Hamaker model

$$v^2 < \frac{H}{4\pi\rho a_0 R^2}$$

*H* — adhesion (Hamaker constant)  
*a<sub>0</sub>* — adhesion distance (~0.4 nm)  
*R* — particle radius  
*ρ* — particle density

- Sieving

$$\text{Restitution coefficient} = \frac{v_2}{v_1}$$

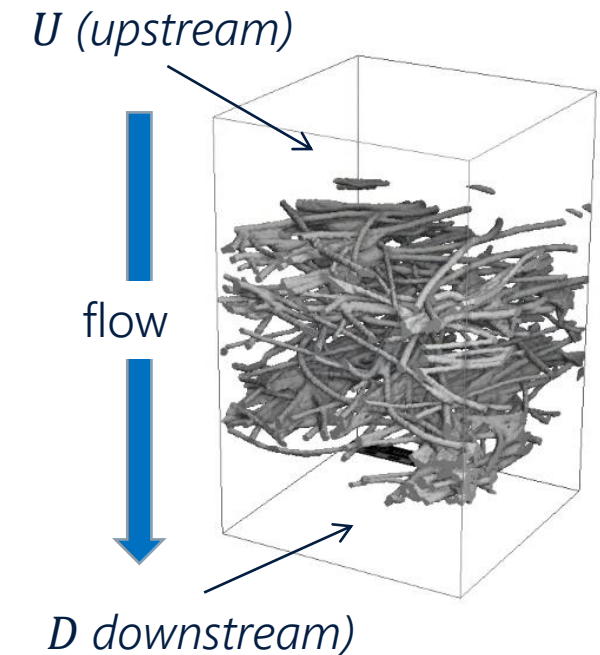
velocity after collision  
initial velocity

[H. Krupp, Advances in Colloid and Interface Sci., 1967, 1 \(2\), 111.](#)

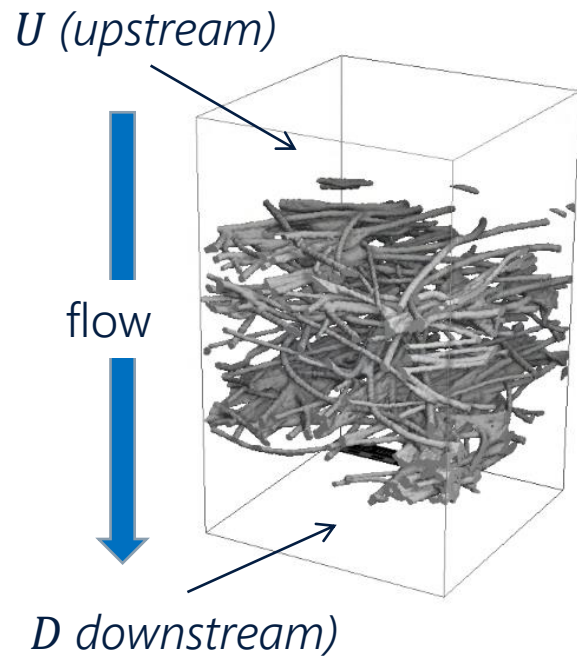
SO, HOW IS FILTER PERFORMANCE  
DESCRIBED?

# DEFINING FILTER PERFORMANCE

- Pressure drop
- Dust holding capacity (DHC)
- Filter efficiency ( $e$ )
  - $\beta$  ratio is efficiency for a given particle size



# FILTER EFFICIENCY AND $\beta$ RATIO



$d$  = particle diameter

Efficiency: 
$$e_d = \frac{n_{d,filtered}}{n_{d,initial}}$$

$\beta$  ratio: 
$$\beta_d = \frac{100}{100 - e_d}$$

$$\beta_d = \frac{n_{d,initial}}{n_{d,D}}$$

$n_{initial}$	$n_D$	$\beta$ ratio	$e$
100,000	50,000	2	50.0 %
100,000	25,000	4	75.0 %
100,000	10,000	10	90.0 %
100,000	5,000	20	95.0 %
100,000	1,000	100	99.0 %
100,000	500	200	99.5 %
100,000	100	1,000	99.9 %

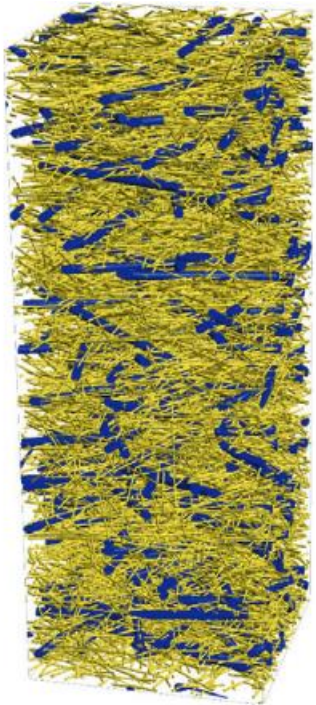
[Hutten, I.M., 2007. "Handbook of Nonwoven Filter Media." Elsevier.](#)

[Math2Market GmbH, Becker, J., Eichheimer, P., Planas, B., 2021. "GeoDict User Guide - FilterDict 2022." Math2Market GmbH, DE.](#)

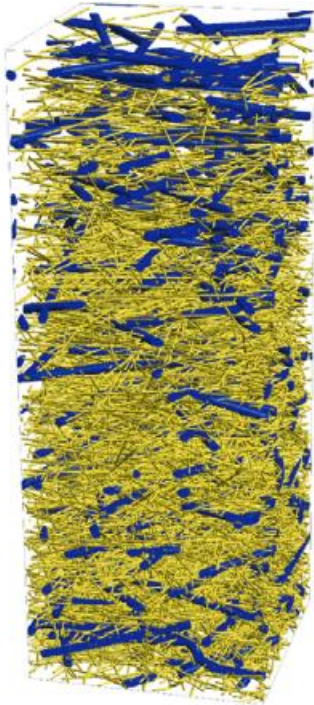


# FILTER LIFETIME EXAMPLE

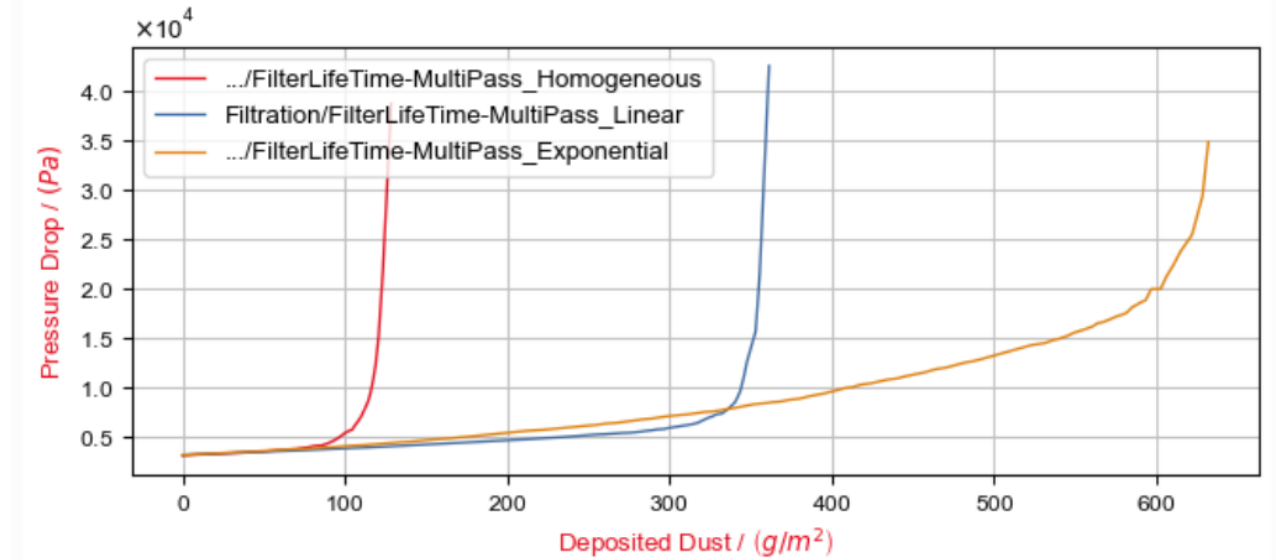
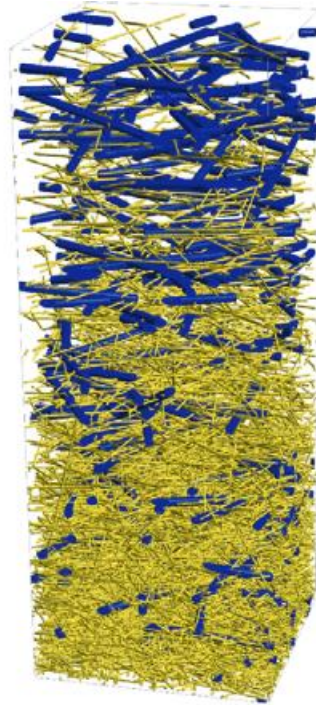
homogeneous



linear



exponential



Microstructure	Pressure drop (10 <sup>4</sup> Pa)	Dust holding (g/m <sup>2</sup> )
Homogeneous	3.867	129
Linear	4.247	361
Exponential	3.477	632

Azimian, M., Kühnle, C., Wiegmann, A., 2018. Chemical Engineering & Technology 41, 928–935.

# THINGS WE COVERED

- How to simulate the filtration process for filter media
- How to track particles during filtration simulations
- How to examine filter efficiency and filter life time

# Q & A SESSION





We'll follow up with your questions.



Recording will be available tomorrow.



Register for the next workshop.

**GEO DICT**  
The Digital Material Laboratory



**USER MEETING  
& WORKSHOPS**

30. Jan. – 03. Feb. 2023

Online

Broad program with presentations and workshops by GeoDict experts from Math2Market and international GeoDict users on

- Image analysis & Image processing for CT-scans, and
- Simulations in the fields of
  - Filtration,
  - Batteries and fuel cells materials,
  - Digital Materials R&D and
  - Digital Rock Physics (DRP) -Digital Core Analysis (DCA).

THANK YOU FOR JOINING US  
SEE YOU NEXT TIME